

STATEMENT If two angles are right angles then they are congruent.

GIVEN: $\angle 1$ IS A RT \angle

$\angle 2$ IS A RT \angle

STATEMENTS

PROVE: $\angle 1 \cong \angle 2$

REASONS
 GIVEN'S
 DEF
 POST
 THM

1. $\angle 1$ IS A RT \angle .

2. $m\angle 1 = 90^\circ$

3. $\angle 2$ IS A RT \angle

4. $m\angle 2 = 90^\circ$

5. $m\angle 1 = m\angle 2$

6. $\angle 1 \cong \angle 2$

1. GIVEN

2. IF RT \angle THEN $m = 90$ (1)

3. GIVEN

4. RT $\angle \rightarrow m = 90$ (3)

5. IF $a = b$ & $b = c$ THEN $a = c$ (24)

6. IF $m = m$ THEN \cong (4)

THEOREM

Statement: If two angles form a linear pair then the angles are supplementary.

Given:

1. $\angle 1$ linear pair $\angle 2$

Prove:

$\angle 1$ SUPPL $\angle 2$

1. $\angle 1$ linear pair

2. $m\angle 1 + m\angle 2 = 180$

3. $\angle 1$ SUPPL $\angle 2$

1. GIVEN

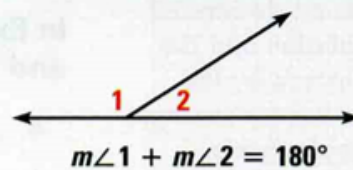
2. IF LINEAR PAIR THEN SUM = 180

3. SUM = 180 \rightarrow SUPPL

POSTULATE

POSTULATE 12 *Linear Pair Postulate*

If two angles form a linear pair, then they are supplementary.

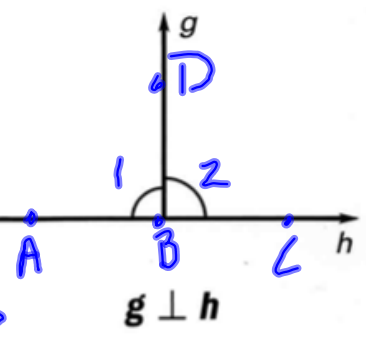


THEOREM 3.1

If two lines intersect to form a linear pair of congruent angles, then the lines are

- a) \perp
- b) \angle s ARE 90°
- c) \angle s ARE RT \angle s

GIVEN: ① $\angle 1 \cong \angle 2$
 ② $\angle 1 \neq \angle 2$
 W/PR
 PROVE: $AC \perp BD$



1. $\angle 1 \cong \angle 2$
 2. $m\angle 1 = m\angle 2$
 3. $\angle 1 \neq \angle 2$ LINEAR PR
 4. $\angle 1$ SUPPL $\angle 2$
 5. $m\angle 1 + m\angle 2 = 180$
 6. $m\angle 1 + m\angle 1 = 180$
 7. $2(m\angle 1) = 180$
 8. $m\angle 1 = 90$ ✓
 9. $\angle 1$ IS A RT \angle ✓
 10. $AC \perp BD$ ✓

∴ $\angle 2$ IS A RT \angle

1. GIVEN ✓
 2. $\cong \rightarrow = m \angle 1$
 3. GIVEN ✓
 4. LINEAR PR \rightarrow 2 \angle s SUPPL (3)
 5. SUPPL \rightarrow SUM \angle s = 180 (4)
 6. SUBSTITUTION (2 \rightarrow 5)
 7. SIMPLIFY (6)
 8. \div PROP = (7, 2)
 9. $m\angle 1 = 90 \rightarrow$ RT \angle (8)
 10. 2 LINES \perp AT RT $\angle \rightarrow \perp$ (9)

∴ SUBSTITUTION (1 \rightarrow 9)

$$\begin{array}{r} m\angle 1 = 90 \\ m\angle 1 = m\angle 2 \\ \hline m\angle 2 = 90 \end{array}$$

$\angle 1$ IS A RT \angle
 $\angle 1 \cong \angle 2$
 $\angle 2$ IS A RT \angle

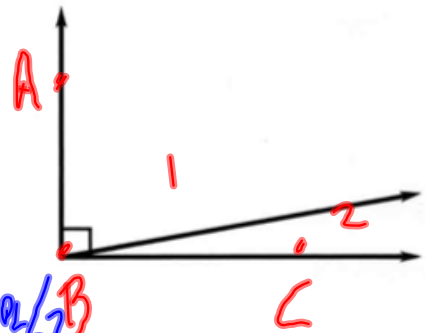
THEOREM 3.2

If two sides of two adjacent acute angles are perpendicular, then the angles are

COMPLEMENTARY

GIVEN: $\overleftrightarrow{AB} \perp \overleftrightarrow{BC}$ PROVE: $\angle 1 \text{ comp } \angle 2$

3.2 PROOF #2



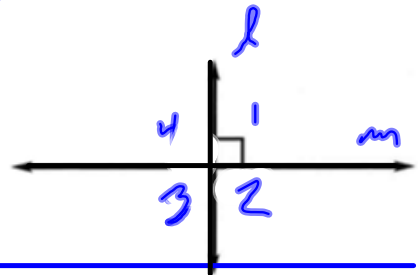
1. $m\angle 1 + m\angle 2 = m\angle ABC$	1. $\angle + \text{Post (D)}$
2. $\overleftrightarrow{AB} \perp \overleftrightarrow{BC}$	2. GIVEN
3. $m\angle ABC = 90$	3. $\perp \rightarrow \text{lines } \perp \text{ at } 90^\circ \angle (2)$
4. $m\angle 1 + m\angle 2 = 90$	4. SUBSTITUTION (3 \rightarrow 1)
$\angle 1 \text{ comp } \angle 2$	4. $\text{sum of } \angle s = 90 \rightarrow \text{comp } \angle (4)$

3.2 Proof # 3

THEOREM 3.3

If two lines are perpendicular,
then they intersect to form

Four RT \angle s. (Four 90° \angle s)



1. $l \perp m$

2. $m\angle 1 = 90$

3. $m\angle 1 = m\angle 3$

4. $m\angle 3 = 90$

5. $m\angle 4 + m\angle 1 = 180$

6. $m\angle 4 + 90 = 180$

7. $m\angle 4 = 90$

1. GIVEN

2. $\perp \rightarrow \perp$ AT $90^\circ \angle$ s (1)

3. VERT \angle s = $m\angle$ (D)

4. TRANSITIVE = (2, 3)

5. \angle + POST (D)

6. SUBSTITUTION (2 \rightarrow 5)

7. - PROP = (6, 90)

